

Unit 5: Quadratic Relations

Day 2: Model Quadratic Relationships

Today we will....

1. Learn how to identify linear and quadratic relationships from their equation
2. Learn how to use DESMOS to find the equation of a curve of best fit.

What Does a Quadratic Look Like?

The graph of a quadratic function is a symmetric, U-shaped curve called a parabola.

A quadratic relation can be modelled in equation form in one of three ways:

- $y = ax^2 + bx + c$ STANDARD FORM
- $y = a(x - s)^2 + k$ VERTEX FORM → use for Desmos
- $y = a(x - s)(x - t)$ FACTORED FORM

We can expand both Vertex and Factored Forms to get Standard Form.

You can factor Standard Form to get Factored Form.

We will be using Vertex Form in Desmos to find the equation of the curve of best fit.

This course does not change Standard Form to Vertex Form (that's for next year!!)

NOTICE:

- A quadratic relation ALWAYS has a squared variable!!
- A linear relation NEVER has a squared variable!!

→ in the expanded form
($y = mx + b$)

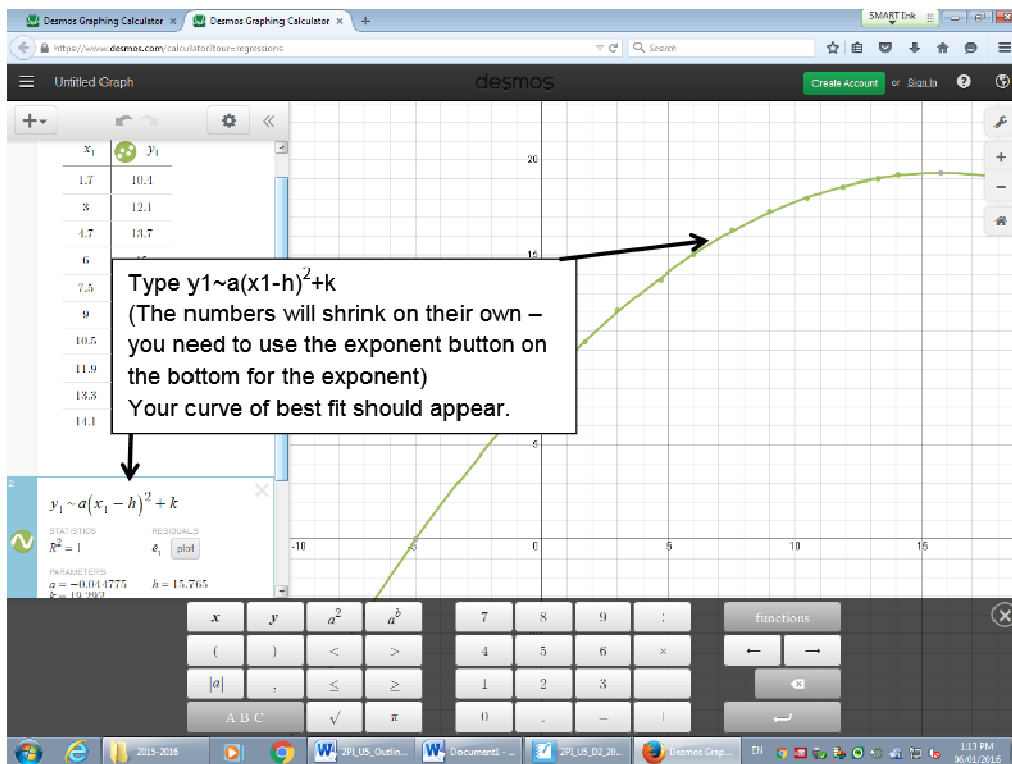
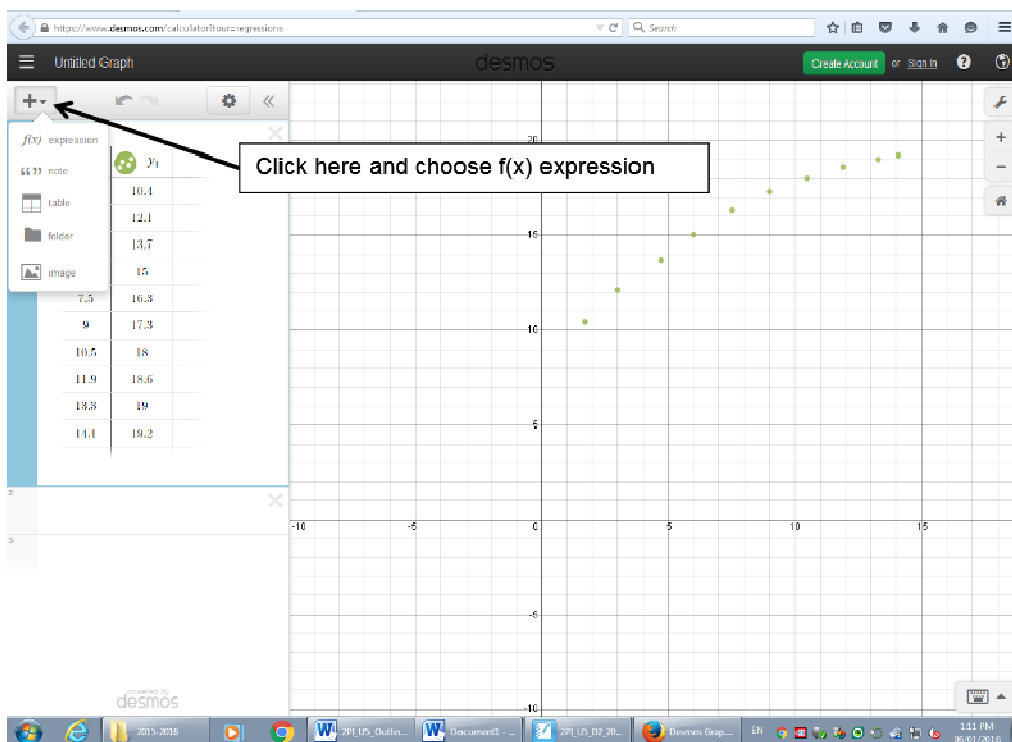
Using DESMOS to find the equation of a quadratic curve of best fit.

Go to www.desmos.com and Launch Calculator

The screenshot shows the Desmos calculator interface. A callout box with the text "Click here and select 'Table'" points to the "+" button in the top-left corner of the graphing area. The interface includes a search bar, a grid, and a calculator keypad at the bottom.

X	Y
1.7	10.4
3	12.1
4.7	13.7
6	15
7.5	16.3
9	17.3
10.5	18
11.9	18.6
13.3	19
14.1	19.2

The screenshot shows the Desmos calculator interface with a scatterplot of the data points from the table. A callout box with the text "Fill in the data to get the scatterplot" points to the data table in the top-left corner. The scatterplot shows a clear upward trend, indicating a positive correlation. The interface includes a search bar, a grid, and a calculator keypad at the bottom.



This box gives you the equation of the curve. The values for a , h and k need to be inserted into the equation.

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$$y_1 \sim a(x_1 - h)^2 + k$$

STATISTICS
 $R^2 = 1$

PARAMETERS
 $a = -0.044775$
 $k = 19.292$

RESIDUALS
 e_1 plot

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We can now write the equation.

You should round decimals to two decimal places:

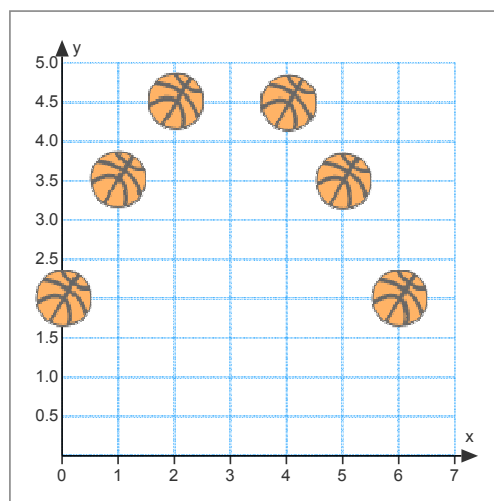
$$y = a(x - h)^2 + k$$

$$y = -0.04(x - 15.77)^2 + 19.29$$

Example 2:

The graph shows the path of a basketball shot. The basketball must not touch the gymnasium ceiling, which is 5.5m high. On this shot, will the basketball touch the ceiling?

X	Y
0	2
1	3.5
2	4.5
4	4.5
5	3.5
6	2



Hint: To solve, find each of the scatterplot points and find the curve of best fit in Desmos. Look at the highest point on your curve - is it higher than 5.5m?

The highest point on the parabola is 4.8m so it does not hit the ceiling

Homework:

Section 6.2 Handout

- whenever the homework says to use a graphing calculator, use Desmos!
- leave equations in Vertex form (what Desmos gives you!)