First Differences: - the differences between the $y$-values that correspond to consecutive $x$-values

- the $\qquad$ of $y$-values with respect to the $x$-values
- if a constant value, the relation is $\qquad$ and the graph is a $\qquad$
- the relation can be represented by $\qquad$
Second Differences: - the difference between consecutive first differences
- for a quadratic relation, second differences are $\qquad$ .
- the relation is quadratic and the graph is a $\qquad$
- the relation can be represented by any form of the quadratic:

$$
\begin{aligned}
& y=a(x-h)^{2}+k(\quad \text { Form }) \\
& y=a x^{2}+b x+c\left(\begin{array}{l}
\text { (__ } \\
y=a(x-s)(x-t) \text { Form })
\end{array}\right. \text { (_ Form) }
\end{aligned}
$$

## Example 1

A snowboarder makes a run by travelling down one side of a parabolic curve and up the other.
The table shows the height of the snowboarder as the distance from the starting point increases.

| Horizontal <br> Distance (m) | Height (m) | First Differences | Second Differences |
| :---: | :---: | :---: | :---: |
| 0 | 10.8 |  |  |
| 1 | 7.5 |  |  |
| 2 | 4.8 |  |  |
| 3 | 2.7 |  |  |
| 4 | 1.2 |  |  |
| 5 | 0.3 |  |  |
| 6 | 0 |  |  |
| 7 | 0.3 |  |  |
| 8 | 1.2 |  |  |
| 9 | 2.7 |  |  |
| 10 | 4.8 |  |  |
| 11 | 7.5 |  |  |
| 12 | 10.8 |  |  |

(a) Is this a quadratic relation? How do you know?
(b) Enter the table into Desmos to find an equation of the curve of best fit.

## Example 2

Use the graph provided to complete the table of values.
Then input the table of values into Desmos to find an equation for the relationship.

| $\mathbf{X}$ | $\mathbf{Y}$ |
| :---: | :---: |
| 0 |  |
| 10 |  |
| 20 |  |
| 30 |  |
| 40 |  |
| 50 |  |
| 60 |  |
| 70 |  |
| 80 |  |
| 90 |  |
| 100 |  |
| 110 |  |
| 120 |  |
| 130 |  |



The equation is:
Why isn't the graph in Desmos exactly like the diagram?

Homework: Section 6.4 Handout

