

Acronyms for Justification

T.P.T. - C.A. - Transversal Parallel Line Theorem
Corresponding Angles (F-pattern)

eg. $\angle A = \angle C$ (T.P.T. - C.A.)
T.P.T. - A.A. - Alternate Angles
(Z-pattern)

eg. $\angle B = \angle D$ (T.P.T. - A.A.)

T.P.T. - C.I.A. - Co-interior Angles (C-pattern)

eg. $\angle E + \angle F = 180^\circ$ (T.P.T. - C.I.A.)

O.A.T. - Opposite Angle Theorem

eg. $\angle G = \angle H$ (O.A.T.)

S.A.T. - Supplementary Angles Theorem

eg. $\angle I + \angle J = 180^\circ$ (S.A.T.)

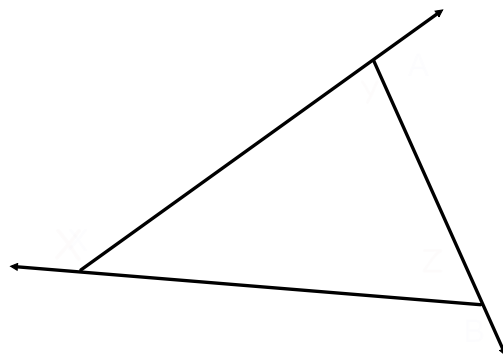
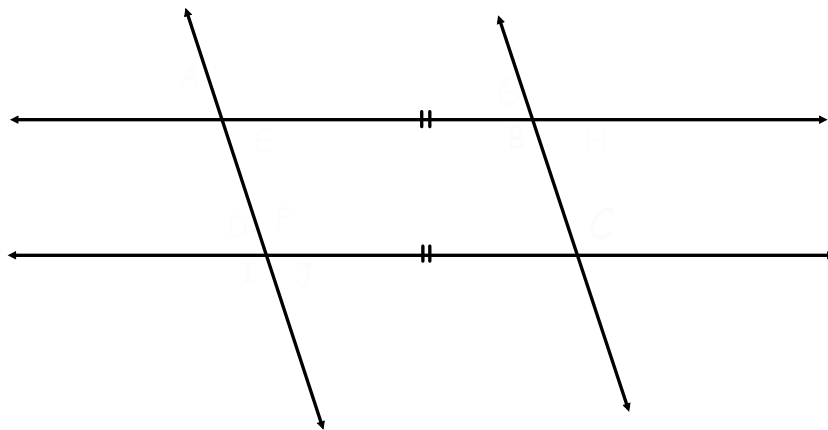
E.A.T. - Exterior Angle Theorem

eg. $\angle X = \angle Y + \angle Z$ (E.A.T.)

P.E.A.S.T - Polygon Exterior Angle Sum
Theorem

eg. $360^\circ = \angle A + \angle B$ (P.E.A.S.T.)

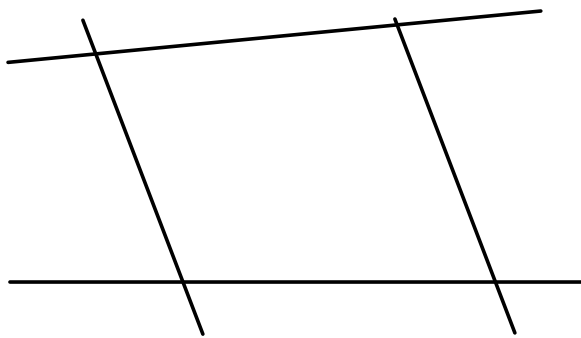
A.S.Q.T. - Angle Sum Quadrilateral Theorem
(Or you may just say ...
sum of interior angles of quadrilateral)



QUADRILATERAL:

Triangle.gsp

1. Draw a large quadrilateral (label vertices)
2. Measure the interior angles
3. Find the sum of the interior angles
4. Draw a line between two non-adjacent vertices (this is called a diagonal).
5. Notice we have created two triangles inside our quadrilateral.
6. Measure and label the 4 exterior angles, then find their sum.



Summary:

1. The sum of the interior angles of a quadrilateral is 360 degrees.

A.S.Q.T. - Angle Sum Quadrilateral Theorem

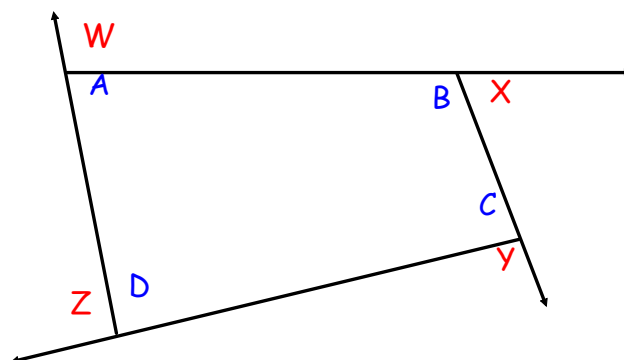
(Or you may just say ...

sum of interior angles of quadrilateral)

$$A+B+C+D=360$$

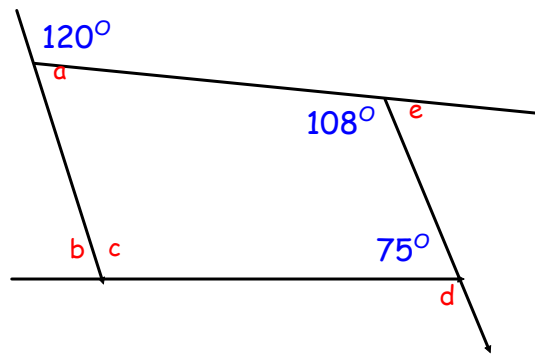
2. The sum of the exterior angles of a quadrilateral is 360 degrees. (P.E.A.S.T)

$$W+X+Y+Z=360$$



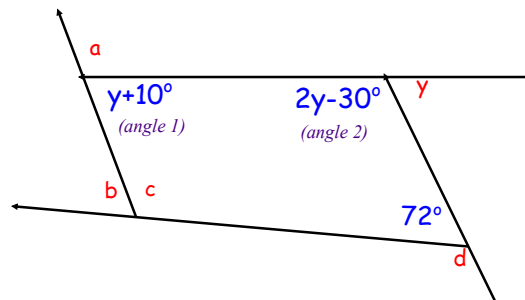
Examples:

1. Find each of the unknown angles:



$$\begin{aligned} \angle e &= 180^\circ - 120^\circ \text{ (Supplementary angles)} \\ &= 60^\circ \\ \angle e &= 180^\circ - 108^\circ \text{ (supplementary angles)} \\ &= 72^\circ \\ \angle d &= 180^\circ - 75^\circ \text{ (supplementary angles)} \\ &= 105^\circ \\ \angle c &= 360^\circ - 60^\circ - 108^\circ - 75^\circ \text{ (sum of interior angles of quadrilateral)} \\ &= 117^\circ \\ \angle b &= 180^\circ - 117^\circ \text{ (supplementary angles)} \\ &= 63^\circ \end{aligned}$$

2. Find the measure of each unknown angle:



Steps:

1. Calculate y :

$$\begin{aligned} y+10^\circ + 2y-30^\circ + 72^\circ + \text{angle } c &= 360^\circ \text{ (Sum of interior angles)} \\ 3y + \text{angle } c &= 258^\circ \\ 3y &= 258^\circ - \text{angle } c \\ y &= 86^\circ - \frac{\text{angle } c}{3} \end{aligned}$$

2. Calculate interior angles:

$$\begin{aligned} \text{angle } 1 &= y+10 & \text{angle } 2 &= 2y-30 & \text{angle } c &= 360-110-80-72 \\ &= 80^\circ & &= 110^\circ & &= 98^\circ \end{aligned}$$

3. Calculate exterior angles:

$$\begin{aligned} \text{angle } a &= 180-80 & \text{angle } d &= 180-72 & \text{angle } b &= 180-98 \\ &= 100^\circ & &= 108^\circ & &= 82^\circ \end{aligned}$$

Attachments

Triangle.gsp