What is "optimization"?

KEY TERM:

Opmizaon: the process of finding values that make a given quanty the

greatest/maximum (or the least/minimum) possible amount

given certain condions.

EX.Ian has a summer job at a fencing company. A customer has purchased 32 secons of prefabricated fencing, each 1 m in length, and wants Ian to create a rectangular pigpen with the <u>largest</u> area possible.

This problem is an example of an opmizaon problem because it asks us to find the dimensions that would **maximize** the rectangular pigpen given a fixed perimeter of 32 m. This is called **opmizing** the area.

Investigation A:

How can you model the maximum area of a rectangle with a fixed perimeter?

EX.Consider the example presented on the previous page, lan needs to find the dimensions of the rectangular pen that will<u>maximize</u> the area with a perimeter of 32 m.

Let's invesgate...

- Start by compleng the table below, tesng different possible dimensions.
 To complete the table.
 - a) Determine the dimensions of 4 different rectangles that Ian could use for this fence.
 - b) Calculate the area of each rectangle.

Width (m)	Length (m)	Perimeter (m)	Area (m²)
2	4	32	58
4	12	32	48
6	10	32	60
8	8	32	64
0	6		60

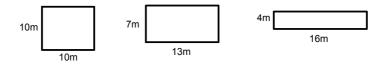
2. REFLECT: What did you find?

- a) What are the dimensions of the rectangle with the maximum, or opmal area? $8 \times 8 \times$
- b) What is the maximum area? 64 ~~
- c) What happened to the area as the length and width became closer in value? The orea increased
- d) Describe the shape of the rectangle with maximum area.



- 3. Suppose the customer decides to use 40 m of fencing instead of 32 m.
 - a) Predict the dimensions of the reclamentar pen with the maximum area.

b) Draw rectangles and find their areas to test your hypothesis.



4. REFLECT:

- a) What is the ideal shape for maximizing the area of a rectangle when given a fixed perimeter?
- b) How can you predict the dimensions of a rectangle with maximum area if you know the perimeter?

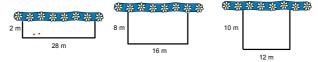
Investigation B:

How can you model the maximum area of a rectangle with a fixed sum of the lengths of only three sides?

EX.Ian's customer decides to use an exisng hedge as one of the boundaries for the pigpen enclosure. This means that he will only use the prefabricated fencing on three sides of the rectangular pen. The client sll wants the pen to have the greatest area possible.



- 1. Ian has 32 m of prefabricated fencing.
 - a) Sketch rectangles to determine the $\,$ dimensions of the rectangle that has the maximum area.



b) Record your results in the table below.

Width (m) よっ	Length (m)	Sum of Lengths of Three Sides (m)	Area (m²)
6	90	32	120
7	١g	35	126
8	16	3.2	198
9	14	32	126
10	12	32	120

2. REFLECT:

- a) What are the dimensions of the rectangular pen with maximum area? $8 \times 16 \times$
- b) Examine the length and width of the enclosure with maximum area. Do any relaonships exist between these dimensions and the dimensions found for a four sided enclosure with same perimeter?

Width was the same Length was doubled

c) Will the hedge allow Ian to enclose more, less, or the same amount of area as before?

the three sides shape allows For more area

Summary:

When Opmizing the Area and Perimeter of a rectangle, there are two possibilies:

- 1. **Four-sided shape:** Make the figure in the shape of a square, with all sides equal in length.
- 2. **Three-sided shape:** Use an exisng wall to create one side of the rectangle. For the remaining three sides, the length is twice as long as the two widths.

Examples:

EX. 1. a) Determine the dimensions of a rectangle with maximum area that

has a perimeter of 60 m.

$$\frac{60}{4} = 15$$
W=15 m

b) Determine the minimum perimeter of a rectangle that has an

EX. 2. Sir Adam Beck PS is adding a rectangular kindergarten playground to the side of the school. The school will form one side of the rectangle. The area of the playground is to be 72 m². Minimizing the perimeter will minimize the cost of the fence. What dimensions use the minimum length of fence?

W:2 W3 w=4 W=5 W6
L=36 L=24 L=18 L=no
L=12

Our langth is 12
and our width is 6