

# MPM 1DI Unit 2

## Polynomials

(Chapter 3 in Textbook!)

### Day 1 - What is a Polynomial? and Working with Exponents

#### **First, a couple of definitions:**

**Term:** "a number or variable or the product of a number and a variable"

E.g. 4 , x , 4x , 15x<sup>2</sup>y are each terms

**Polynomial:** "an expression containing one or more terms"

E.g. 4x<sup>2</sup>y + 3x - 5

\*NOTE: a POLYNOMIAL cannot have a variable in the denominator of a fraction.

E.g.  $\frac{4}{x}$  is not a term in a polynomial (though it is a term!)

**Types of Polynomials:**

Polynomials are classified by the number of terms:

Name	Number of Terms	Example
Monomial	1	x
Binomial	2	2y + c
Trinomial	3	2y + c + x

like term - same variable same exponent

**Degree of Polynomials:**

The degree of a polynomial refers to:

Example: What is the degree of:

- a)  $5x^2$     b)  $4$     c)  $3x^2y^1$
- = 2        = 1        = 3

d)  $5xy + 3x^2 - 2x^3y^5$

↑        ↑        ↑

2        2        8

= 8

Example 1: Expand and then Evaluate:  $\frac{49}{343}$

a)  $\left(\frac{3}{4}\right)^4$         b)  $\left(-\frac{3}{7}\right)^3$         c)  $(0.3)^3$

=  $\frac{3^4}{4^4}$                 =  $\frac{3 \times 3 \times 3}{7 \times 7 \times 7}$         =  $0.3 \times 0.3 \times 0.3$

=  $\frac{3 \times 3 \times 3 \times 3}{4 \times 4 \times 4 \times 4} = \frac{81}{256}$         =  $\frac{-27}{343}$                 = 0.027

Example 2: Solve the following equations involving exponents:

Given the equation  $h = (t - 5)^3 - t^2 + 3(t - 1) - 2$ , solve for h when:

i)  $t = -3$      $h = (-3 - 5)^3 - (-3)^2 + 3(-3 - 1) - 2$

$h = (-8)^3 - (-3)^2 + 3(-4) - 2$

$h = -512 - (9) + 3(-4) - 2$

$h = -512 - (9) - 12 - 2$

$h = -512 - 9 - 12 - 2$

$h = -521 - 12 - 2$

ii)  $t = 2$

$h = -533 - 2$

$h = -535$

Example 3: Evaluate each of the following (don't forget order of operations)

$$\begin{array}{l}
 \text{a) } (4^2 - 3^2) + (4^3 - 3^4) \\
 = (16 - 9) + (64 - 81) \\
 = 7 + -17 \\
 = -10
 \end{array}$$

$$\begin{array}{l}
 \text{b) } \left(\frac{2}{3}\right)^2 + \left(\frac{3}{4}\right)^3 \\
 = \left(\frac{2 \times 2}{3 \times 3}\right) + \left(\frac{3 \times 3 \times 3}{4 \times 4 \times 4}\right) \\
 = \frac{4}{9} + \frac{27}{64} \quad \underline{\text{LCD}}
 \end{array}$$

$$\begin{array}{r}
 64 \\
 \times 9 \\
 \hline
 576
 \end{array}$$

$$\begin{array}{l}
 = \frac{4 \times 64}{576} + \frac{27 \times 9}{576} \\
 = \frac{256}{576} + \frac{243}{576} \\
 = \frac{499}{576}
 \end{array}$$